

$$\begin{aligned}
f_1(\theta_1, \theta_2, \varphi) &= \cos^2 \theta_1 \cos^2 \theta_2 \\
f_2(\theta_1, \theta_2, \varphi) &= \frac{1}{2} \sin^2 \theta_1 \sin^2 \theta_2 (1 + \cos 2\varphi) \\
f_3(\theta_1, \theta_2, \varphi) &= \frac{1}{2} \sin^2 \theta_1 \sin^2 \theta_2 (1 - \cos 2\varphi) \\
f_4(\theta_1, \theta_2, \varphi) &= \frac{1}{2\sqrt{2}} \sin 2\theta_1 \sin 2\theta_2 \cos \varphi \\
f_5(\theta_1, \theta_2, \varphi) &= \frac{-1}{2\sqrt{2}} \sin 2\theta_1 \sin 2\theta_2 \sin \varphi \\
f_6(\theta_1, \theta_2, \varphi) &= -\sin^2 \theta_1 \sin^2 \theta_2 \sin 2\varphi \\
\int_{-1}^1 \sin 2\theta d(\cos \theta) &= \int_{-1}^1 2\sin \theta \cos \theta d(\cos \theta) = \\
= \int_{-1}^1 2\sqrt{1 - \cos^2 \theta} \cos \theta d(\cos \theta) &= -\frac{2}{3} (1 - \cos^2 \theta)^{3/2} \Big|_{-1}^1 = 0 \\
\int_{-1}^1 \cos^2 \theta d\cos \theta &= \frac{1}{3} \cos^3 \theta \Big|_{-1}^1 = \frac{2}{3} \\
\int_{-1}^1 \sin^2 \theta d\cos \theta &= \int_{-1}^1 (1 - \cos^2 \theta) d\cos \theta = \\
= (\cos \theta - \frac{1}{2} \cos^3 \theta) \Big|_{-1}^1 &= 2 - \frac{2}{3} = \frac{4}{3} \\
f_1(\varphi) &= \frac{4}{9} \\
f_2(\varphi) &= \frac{4}{9} (1 + \cos 2\varphi) \\
f_3(\varphi) &= \frac{4}{9} (1 - \cos 2\varphi) \\
f_4(\varphi) &= 0 \\
f_5(\varphi) &= 0 \\
f_6(\varphi) &= -\frac{16}{9} \sin 2\varphi
\end{aligned}$$